

All problems are to be written up clearly and thoroughly, using complete sentences. This assignment is due in discussion at 2pm on Thursday, April 18th.

For all T/F problems on the homework, provide a brief justification for your answer. That may be citing an appropriate theorem or providing a counterexample.

1. Section 1.4 problems 1, 3 d, 4 e, 6 (as long as  $\mathbb{F}$  does not have characteristic 2), 7, 8 (Here  $P_n(F)$  is the set of polynomials of degree less than or equal to  $n$  with coefficients in a field  $\mathbb{F}$ ), 9, 10, 11, 12, 13
2. Section 1.5 problems 1, 2 a, c, e, 4, 5, 6, 8, 9, 11, 15, 16, 18, 20
3. Let  $\mathbb{C}[x]$  be the vector space of polynomials and let  $W = \text{span}\{x^a \mid a > 2\}$ .
  - (a) Find a set of three linearly independent elements of the quotient space  $\mathbb{C}[x]/W$  (see Section 1.3 problem 31).
  - (b) Find two nonzero elements  $p(x), q(x) \in \mathbb{C}[x]$  that are linearly independent in  $\mathbb{C}[x]$  but where  $p(x) + W$  and  $q(x) + W$  are linearly dependent and both nonzero in  $\mathbb{C}[x]/W$ .